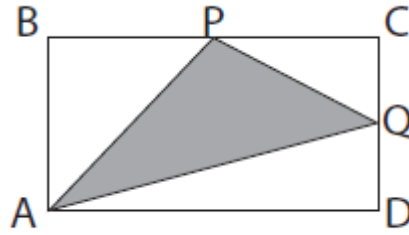


1. In rectangle  $ABCD$ ,  $P$  is the midpoint of side  $BC$  and  $Q$  is the midpoint of  $CD$ . The area of  $\triangle APQ$  is what fractional part of the area of rectangle  $ABCD$ ?
- 在長方形 $ABCD$ 中， $P$ 是邊 $BC$ 的中點， $Q$ 是 $CD$ 的中點。問 $\triangle APQ$ 的面積佔長方形 $ABCD$ 的面積的幾分之幾？



2. Find the value of integral part of  $\sqrt{1+3+5+\dots+45+47+49}$ .
- 求 $\sqrt{1+3+5+\dots+45+47+49}$ 的整數部分。
3. How many degrees are in the angle formed by the hands of a clock at 8:24?
- 在8:24時，求時針和分針的夾角。
4. How many different triangles can be formed whose 3 vertices are chosen from the rectangular array of 8 points shown?
- 在以下八個點中，以其中三點作為三角形的三隻角，問可以形成多少個三角形？



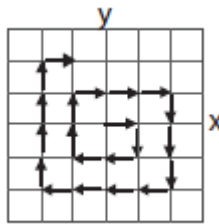
5. Line segments form a path that starts at  $(0,0)$ , is drawn to  $(1,0)$ , and then to  $(1,2)$ . Each new segment forms a right angle with the segment before it and is 1 unit longer than that segment. The path ends at  $(0,0)$ . How many segments are in the shortest possible path?
- (Hint: Consider horizontal and vertical segments separately.)
- 線段由 $(0,0)$ 畫至 $(1,0)$ ，再畫至 $(1,2)$ 。每一條線段的長度都垂直之前每一條線段，而且比它長1單位。最後路線在 $(0,0)$ 結束。問在最短的路線中，最少有多少條線段？
- (提示：分開考慮水平線和垂直線)
6. 561 is the product of 3 different prime numbers. How many factors of 561 are not prime?
- 561是3個不同質數的乘積。問561的因數中有多少個是非質數？

7. The first three terms in a sequence are: 1, 2, 3. Each term after that is the opposite of the sum of the three previous terms. For example, the 4<sup>th</sup> term is  $-6$  (the opposite of  $1+2+3$ ), and the 5<sup>th</sup> term is 1. What is the 99<sup>th</sup> term?

在某數列中，首三項是1, 2, 3。然後接著每一項都是之前三項之和的相反數。例如，第四項是 $-6$ ( $1+2+3$ 的相反數)，而第五項是6。問第99項是多少？

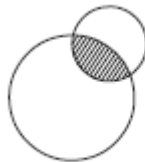
8. The picture shows a “spiral” that begins at the origin (0,0) and passes through every lattice point in the plane. Each small arrow is 1 unit in length. Following the “spiral”, what is the length of the path from the origin to the point (5,3)?

下圖顯示了一個「螺線」，它在(0,0)開始，然後經過平面上每一交點。每一個小箭頭都長一單位。問由(0,0)開始至(5,3)，路徑長多少？



9. A circle with radius 5 cm intersects a circle with radius 3 cm as shown. The area of the shaded region is  $\frac{7\pi}{2}$  square cm. Find the total combined area inside the circles, but outside the shaded region. Leave your answer in terms of  $\pi$ .

在下圖中，一個半徑5厘米的圓相交一個半徑3厘米的圓。陰影部分的面積是 $\frac{7\pi}{2}$ 平方厘米。如果不包括陰影部分，兩圓共佔的面積是多少平方厘米？答案以 $\pi$ 表示。



10. Starting with 1, Sara lists the counting numbers in order but omits all those that use the digit 9. What is the 300<sup>th</sup> number on her list?

由1開始，薩拉列出所有數位不包括9的數字，問第300個數字是多少？